

PROB

7/17/19 p1

$$P((A \cup B)^c) = P(A^c \cap B^c)$$

~~DICE~~

$$A = \text{EVEN} = \{2, 4, 6\} \quad \frac{1}{2}$$
$$B = \text{PRIME} = \{2, 3, 5\} \quad \frac{1}{2}$$
$$A \cup B = \{2, 3, 4, 5, 6\} \quad \frac{5}{6}$$

$$(A \cup B)^c = \{1\} \quad P = \frac{1}{6}$$

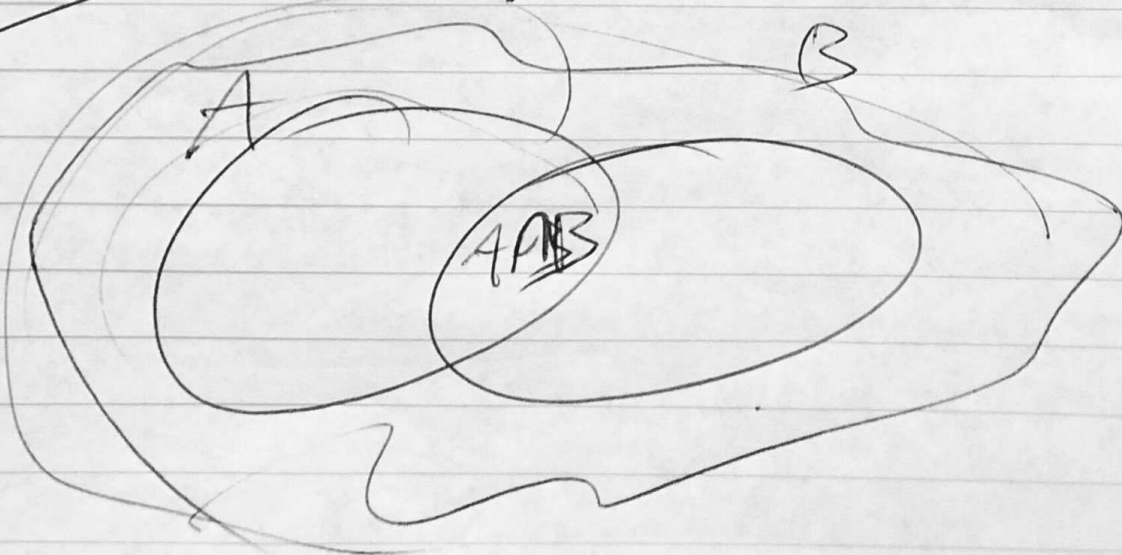
$$A^c = \{1, 3, 5\} \quad P = \frac{1}{2}$$

$$B^c = \{1, 4, 6\} \quad P = \frac{1}{2}$$

$$A^c \cap B^c = \{1\} \quad P = \frac{1}{6}$$

PROOF

VENN



Q H F

2

$$P(Q \cup H \cup F) = P(Q) + P(H) + P(F)$$

$\frac{1}{3}$
 $\frac{1}{4}$
 $\frac{1}{3}$

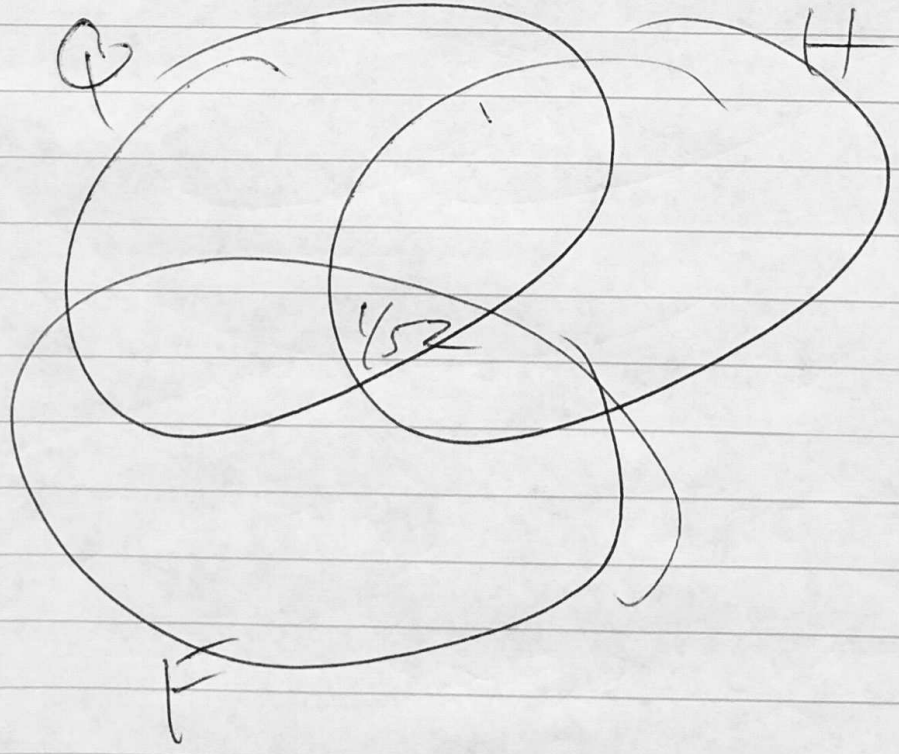
$$- P(Q \cap H) - P(Q \cap F) - P(H \cap F)$$

$\frac{1}{52}$
 $\frac{1}{13}$
 $\frac{1}{13}$

$$+ P(Q \cap H \cap F)$$

$\frac{1}{52}$

$$P = \frac{1}{52} (4 + 13 + 16 - 1 - 4 - 4 + 1) = \frac{25}{52} ?$$



HALF LIFE 1 sec

3

t -LIFE OF AN Na^{26} ATOM

$$P(t > 1) = \frac{1}{2}$$

$$P(t > 2) = \frac{1}{4}$$

$$P(t > t_0) = \frac{1}{2^{t/t_0}} = 2^{-t/t_0}$$

$$t_0 = 0$$

$$P = 1$$

EXPONENTIAL

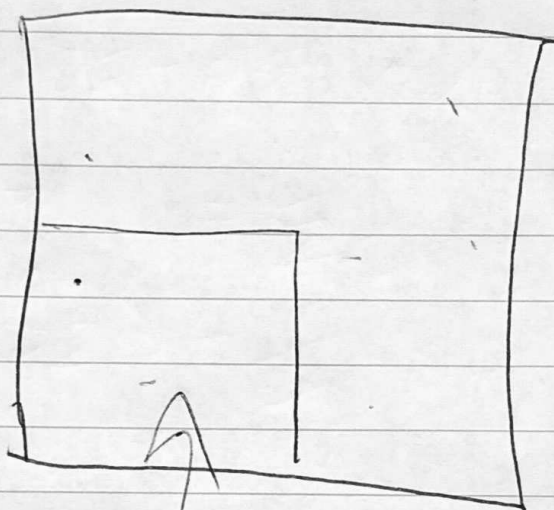
$$t_0 = 1$$

$$P = \frac{1}{2}$$

$$P(t_0 < t < t_1) = \frac{1}{2^{t_1/t_0}} - \frac{1}{2^{t_0/t_0}}$$

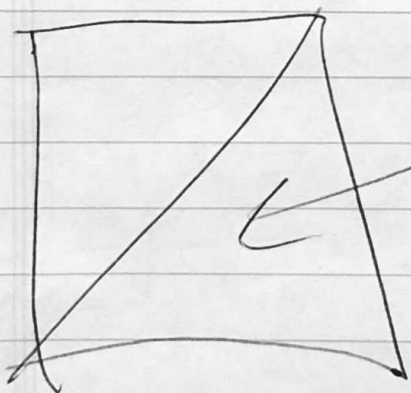
Ex 3.14

4



$$P = \frac{1}{4}$$

$$P(0 \leq x \leq \frac{1}{2} \text{ \& } 0 \leq y \leq \frac{1}{2})$$



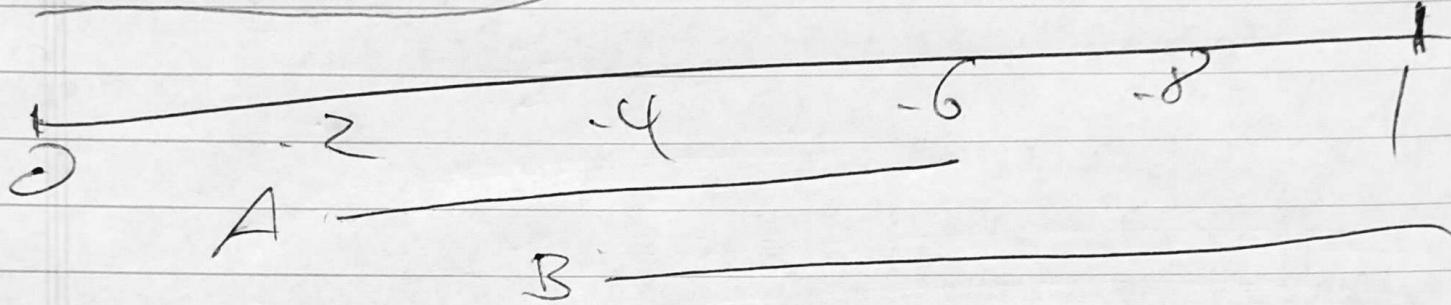
$$P = \frac{1}{2}$$

100CLICKER

5

$A \cup B^c$

B^c



$A \cup B$

$$.2 \leq x \leq 1 \quad P = .8$$

$$P(a \leq x \leq b) = b - a$$

e_1 : 1st BIT ARRIVES OK 6

e_2 2nd

e_3 3rd

$$P(e_1) = .9 = P(e_2) = P(e_3)$$

$$P(e_1 e_2 e_3) = .9 \times .9 \times .9 = .9^3 = .729$$