

11/31/19 - 1

$$P(U) = .005$$

$$P(\bar{U}) = .995$$

$$P(+|U) = .99$$

$$P(-|\bar{U}) = .99$$

$$P(A|B)P(B) = P(A \cap B)$$

WANT $P(U|+) = \frac{P(U \& +)}{P(+)}$

$$P(n \& +) = P(+|n)P(n) = .99 \times .005 = .005$$

$$P(\bar{n} \& +) = P(+|\bar{n})P(\bar{n}) = .01 \times .995$$

$$P(+)= .005 + .01 = .015 \quad \text{--- } .01$$

$$P(U|+) = \frac{.005}{.015} = \frac{1}{3}$$

	# MADE	\$ BAD	# BAD
A	20,000	5%	1,000
B	30,000	3%	900
C	50,000	1%	500
	<u>100,000</u>		<u>2,400</u>

2

$$P(A | \text{BAD}) = \frac{1000}{2400} = \frac{1}{2.4}$$

$$P(B | \text{BAD}) = \frac{9}{24}$$

$$P(C | \text{BAD}) = \frac{5}{24}$$

$$P_n(k) = \binom{n}{k} p^k (1-p)^{n-k}$$

COMBINATION CHOOSE $\binom{n}{k} = \frac{n!}{k!(n-k)!}$

4 TOSSES OF FAIR COIN $n=4, p=\frac{1}{2}$

$$\binom{4}{0} = \frac{4!}{4!0!} = 1 \quad \binom{4}{1} = \frac{4!}{3!1!} = 4 \quad \binom{4}{2} = 6 \quad \binom{4}{3} = 4$$

$$\binom{4}{4} = 1$$

$$\sum_{k=0}^4 \binom{4}{k} = 1 + 4 + 6 + 4 + 1 = 16$$

$$= 2^4$$

$$P(0 \text{ HEADS}) = \binom{4}{0} p^0 (1-p)^4 = \frac{1}{16}$$

$$P(1 \text{ HEAD}) = \binom{4}{1} \left(\frac{1}{2}\right) \left(\frac{1}{2}\right)^3 = \frac{4}{16}$$

$$P(2 \text{ HEADS}) = \frac{6}{16} = .375$$

UNFAIR $p = .1$

$$P(2 \text{ HEADS}) = P_4(2) = \binom{4}{2} \cdot .1^2 \cdot .9^2 = 6 \times .0081 = .05$$

$$P_4(1) = \binom{4}{1} \cdot .1 \cdot .9^3 = 4 \times .729 \approx .29$$

$$P_4(0) = .9^4 \approx .6$$

TOSS A FAIR DIE 6 TIMES.

WANT PROB WE SAW EACH FACE ONCE

$$P = \binom{6}{1\ 1\ 1\ 1\ 1\ 1} \left(\frac{1}{6}\right)^6 = 6! \left(\frac{1}{6}\right)^6 = \frac{6!}{6^6}$$

PROB (WE SEE ONE 1, 2-2, 3-3, 0-0)

$$P = \binom{6}{1\ 2\ 3\ 0\ 0\ 0} \left(\frac{1}{6}\right)^6 = 60 \cdot \left(\frac{1}{6}\right)^6 = \frac{720}{1 \cdot 2 \cdot 6 \cdot 1 \cdot 1 \cdot 1} = 60$$