

2/28/19 - 1

R.V. $0 \leq x \leq 1$

$$f(x) = \begin{cases} 1 & \text{if } 0 \leq x \leq 1 \\ 0 & \text{otherwise} \end{cases}$$

$$P[a < X < b] = b - a \quad 0 \leq a \leq b \leq 1$$

$$P[.6 \leq X \leq .7] = .1$$

SUPPOSE X WAS FEET.

WE WANT CM.

$$Y = 30X$$

$$f(Y) ?$$

$$X = .5 \text{ FT}$$

$$Y = 15 \text{ CM}$$

$$P[10 \leq Y \leq 20] = P\left[\frac{1}{3} \leq X \leq \frac{2}{3}\right]$$

$$= f(Y) (20 - 10)$$

$$= \frac{1}{3}$$

$$= 10 f(Y)$$

$$f(Y) = \frac{1}{30}$$

$$\frac{f'(y)}{f(x)} = \frac{dx}{dy} = \frac{1}{30}$$

EXPONENTIAL DISTV

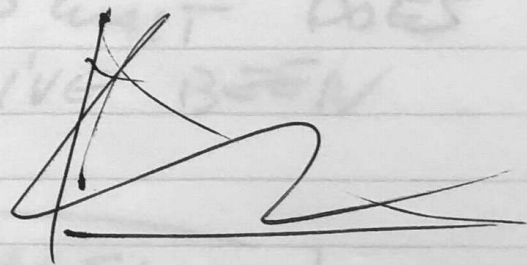
$$P[X > a] = e^{-\lambda a} \quad a \geq 0$$

$$\text{CDF } P[X \leq a] = 1 - e^{-\lambda a}$$

$$\text{PDF} = \frac{d \text{CDF}}{da}$$

$$\frac{d(1 - e^{-\lambda a})}{da} = \lambda e^{-\lambda a}$$

MEMORYLESS



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$$P[X \geq b+a | X \geq a]$$

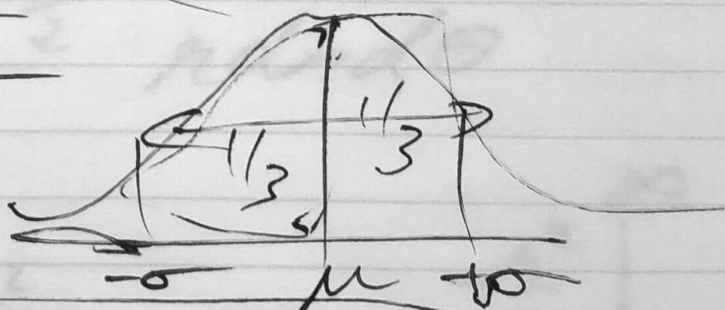
$$= \frac{P[X \geq b+a \text{ and } X \geq a]}{P[X \geq a]}$$

$$= \frac{P[X \geq b+a]}{P[X \geq a]} = \frac{e^{-\lambda(b+a)}}{e^{-\lambda a}} = e^{-\lambda b}$$

HOW LONG I STILL HAVE TO WAIT DOES NOT DEPEND ON HOW LONG I'VE BEEN WAITING.

NORMAL (GAUSSIAN)

2 PARAMS: μ, σ



$$\mu = 0$$

$$\sigma = 1$$

$$f(x) = \frac{1}{\sqrt{2\pi}} e^{-\frac{x^2}{2}}$$

48

SHOW

$$\int_{-\infty}^{\infty} f(x) dx = 1$$

$$\text{LET } A = \int_{-\infty}^{\infty} f(x) dx = \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{\infty} e^{-\frac{x^2}{2}} dx$$

$$A^2 = \frac{1}{2\pi} \int_{-\infty}^{\infty} e^{-\frac{x^2}{2}} dx \int_{-\infty}^{\infty} e^{-\frac{y^2}{2}} dy$$

$$= \frac{1}{2\pi} \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} e^{-\frac{(x^2+y^2)}{2}} dy dx$$

CHANGE VARIABLES $\rightarrow (r, \theta)$

$$= \frac{1}{2\pi} \int_0^{\infty} \int_0^{2\pi} e^{-\frac{r^2}{2}} r dr d\theta$$

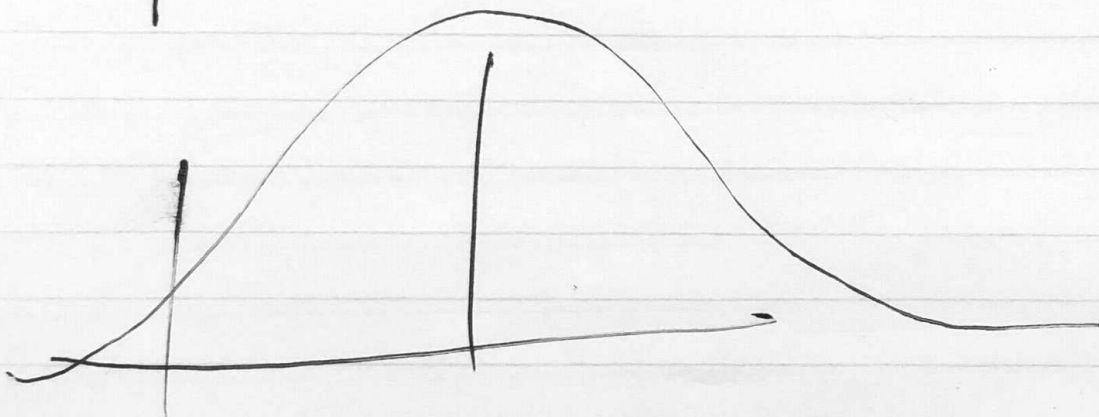
$$= \int_0^{\infty} r e^{-\frac{r^2}{2}} dr = -e^{-\frac{r^2}{2}} \Big|_0^{\infty} = 1$$

5*

N NORMAL $N(\mu, \sigma)$
0 2

N NORMAL $(0, 2)$
 μ σ

$$P[N \leq -\sqrt{2}V] = 10^{-6}$$

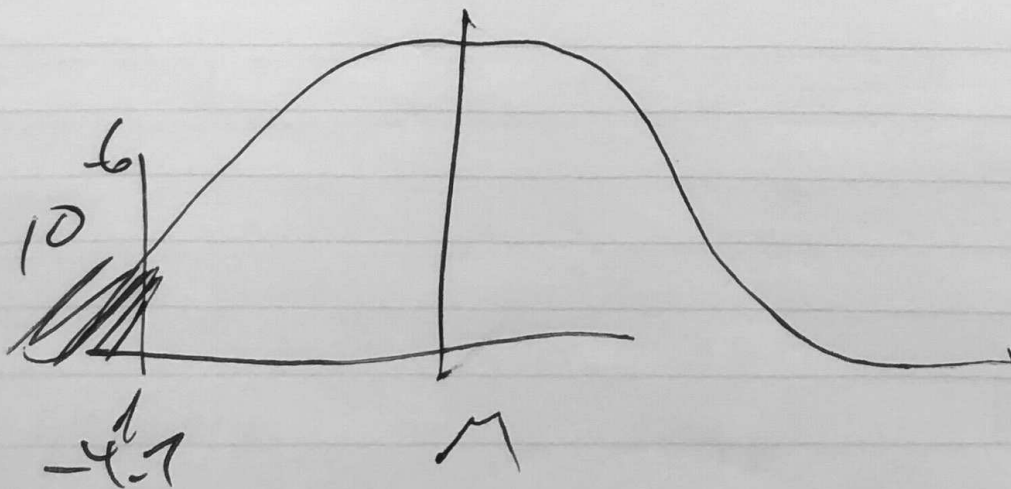


DEFINE A NEW NORMAL R.V.

$$M = \frac{N}{\sqrt{2}}$$

M HAS $\sigma = 1$

$$P[M \leq -\sqrt{2}V] = 10^{-6}$$



$$\frac{10}{2} = 4,7 \quad \text{kor}$$

$$\frac{10}{200} = 4,7 \quad V = 900$$